NUMERICAL SIMULATION ON FLOW AND HEAT TRANSFER IN OSCILLATING HEAT PIPES

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ABSTRACT

In order to predict the heat transport capability of oscillating heat pipes (OHPs), a mathematical and physical model of OHP was built to simulate the process of flow and heat transfer in vertical bottom heating mode. Water was used as working fluid. Mixture model in FLUENT was used for two-phase flow numerical simulation. The result showed that the numerical simulation was successful to reproduce the behavior of the internal flow of OHP, including vapor generation in evaporation section, oscillation phenomena caused by the pressure difference and heat transfer due to oscillation. Comparing with the experimental tests, the simulation results agreed with the experimental records fairly well.

Keywords: oscillating heat pipes (OHPs), numerical simulation, heat transfer, flow, predicting correlation

1. INTRODUCTION

An oscillating heat pipe (OHP) is a two-phase flow device used for transferring heat without any moving mechanical parts (Akachi and Polášek, 1996; Polášek and Zelko, 1997). It consists of tubes/channels of capillary dimensions arranged in a serpentine manner and joined end to end as shown in Fig.1. It is predicted as one of the most promising solution for higher heat dissipation compact cooling. The heat transfer characteristics of OHPs have become a hot research. However, most studies focused on the experimental investigations. Only a few researches paid attention to the numerical simulations. Zuo (Zuo et al., 2001) simulated the operation of vapor and liquid slugs in OHP by the single spring-mass-damper system, which was far away from the experimental results. Wong (Wong et al., 1999) predicted the direction of vapor and liquid slugs by the multiple spring-mass-damper system, but without considering the effect of heat exchange. Dobson (Dobson, 2004) and Faghi et al. (Shafii et al., 2002; Zhang et al., 2002) established the mass, momentum and energy conservation equations of OHP by the control volume method. Khandekar (Khandekar et al., 2002) proposed an artificial neutral network to predict the thermal performance of OHP, which based on an amount of experimental data. In fact, there was still no an effective numerical simulation to predict the thermal performance of OHPs successfully.

With the aim of exploring potential applications of OHP technology, it is very important to predict the thermal performance of OHP by the numerical simulation, rather than by a large number of experiments. In this work, a mathematical and physical model of OHP was built to simulate the process of flow and heat transfer. The simulation results were compared with the experimental results.

2. EXPERIMENTAL APPARATUS AND PROCEDURE

In the experiments, an experimental apparatus of OHPs were established for thermal performance test to study the flow and heat transfer. The four-turn OHP was selected as a typical shape. Pure water was used as working fluid. The operational orientation was vertical bottom heating mode.

Fig. 1 Prototype of OHP

In the thermal performance test, two types of copper tubes with outer diameter ($D_o$) of 2.5 and 3mm, inner diameter ($D_i$) of 1.3 and 1.8 mm were used as manufacturing material to be bent into the OHPs respectively. The heat transfer length ($L$) of 200 mm were adopted for comparative experiments. In the liquid filling process, internal channels of copper tubes were first exhausted and the working fluid was filled fully into the tube under the pressure difference. Liquid filling ratio was controlled around 50±5% by the second vacuum, which discharged the excess liquid. The experimental apparatus of OHPs was shown in Fig. 2. The nickel chrome electric wires were wound around the copper tube,
which was wrapped in thermal insulation adhesive plaster, as evaporation section. They were connected to the transformer, which supplied heating power by adjusting the current and voltage. The length of evaporation section was 20 mm, the same as the condensation section; and the condensation section was cooled by water (25±0.05°C). The OMEGA K-type thermocouples were installed to measure the wall temperature at different positions of OHPs. The detailed location of thermocouples was shown in Fig. 2. The pulse of temperature was measured to reflect the internal working fluid oscillation indirectly.

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All tests were conducted at an ambient temperature of 25±1°C. Based on the application requirements, when the average temperature of evaporation section was over 100°C, the experiment would be stopped. The thermal resistance of OHPs was equal to temperature difference between condensation section and evaporation section divided by heating power.

\[ R_{OHP} = \frac{T_e - T_c}{Q_h} \]  

\( R_{OHP} \): thermal resistance of OHP; \( T_e \): average temperature of \( T_1, T_2, T_3 \) and \( T_4 \) approximately instead of evaporation section; \( T_c \): average temperature of \( T_{13}, T_{14}, T_{15} \) and \( T_{16} \) approximately instead of condensation section; \( Q_h \): heating power.

3. DESCRIPTION OF SIMULATION

3.1 Physical model

The 2D physical model was built to simulate the internal flow and heat transfer in OHPs, shown in Fig. 3. Pure water was used as working fluid. The internal flow of OHP was mainly vapor-liquid two phase flow. It was assumed that the density of liquid phase was incompressible, and the vapor phase was compressible. The phase and density changed with the temperature changed. The geometric model and mesh diagram were shown in Fig. 3. The design length of evaporation section was 20 mm, and the length of condensation section was 20 mm.

3.2 Definite conditions

As the OHP was operated in a negative pressure, we assumed that the water vaporization temperature is 50°C according to the experimental condition. It meant that the liquid phase of working fluid evaporated over 50°C and the vapor phase condensed below 50°C. The heat flux in evaporation section depended on the power input. The heat transfer coefficient in condensation section was set according to the actual situation. The insulation section was set to insulation boundary condition.

In the cases, mixture model was used for flow and heat transfer simulation. The user-defined function was added to calculate mass and energy transport, in order to achieve heat transfer process of evaporation and condensation.

4. SIMULATION ON START-UP PROCESS

In the simulation case, the four-turn OHP with inner diameter \( (D_i) \) of 1.3 and heat transfer length of 200 mm was selected as 2D model for comparison. The heating power was 24 W. As shown in Fig. 4, the start-up of OHP had been recorded, which went through the process of heat transfer. From 1 s to 5 s, the temperature in evaporation section increased due to power input. When the time up to 7 s, the evaporation section reached a certain temperature, the generation of bubbles began. The region of high temperature in evaporation section was expanding from 7 s to 9 s. As the temperature increased, the bubbles jetted across the evaporation section to the condensation section. High temperature
The quasi periodic thermal oscillation with the same characteristic frequency for both evaporation section and condensation section, indicates heat transfer due to oscillation process.
OHP startup process (the total time is 35 seconds) was recorded. It was found that when the hotwall (marked in Fig.3) reaches a certain temperature (about 75°C), the temperature oscillation began. The oscillation amplitude and temperature difference between evaporation and condensation section was decreasing with the startup of OHP. The quasi periodic thermal oscillation with the same characteristic frequency appeared in both evaporation section and condensation section, which indicated heat transfer due to oscillation process. Comparing to the experimental records in Fig.6, the trend of temperature change in simulation was consistent with experimental results.

5. NUMERICAL SIMULATION COMPARED WITH EXPERIMENTAL RESULTS

5.1 Comparison of temperature curves

In the case, the OHP with inner diameter of 1.3mm and heat transfer length of 200mm was selected for comparison between simulation and experimental results. Fig.7 was the temperature record for OHP performance test in 24W; while Fig. 8 was the temperature record for OHP 2D simulations in 24W. As can been seen in Fig.8, the oscillation range in temperature was consistent with the experimental record. The average temperature of the experimental record in evaporation section was about 57°C; while condensation section’s was about 32°C. The average temperature of 2D simulation record in evaporation section was about 63°C; while condensation section’s was about 28°C.

The simulation temperature was slightly higher than the experimental record, but it represented the simulation model was successful to predict the OHP performance and operation. Furthermore, it was noticed that the simulation record needed some time to develop into the stable oscillation state after the startup process. In contrast, the experimental record reached the stable oscillation state earlier. Therefore, the longer simulation, the more accurate results can be obtained, closer to the real operation.

5.2 Comparison of thermal resistance

After the section discussed above, it proved that 2D mathematical model could successfully simulate the internal flow of an OHP. In this section, several cases with different parameters were selected for comparison in different operating conditions. As can be seen in Fig.9, the thermal resistance of 2D model simulation was higher than the test data. From the comparison of fitting equations between 2D simulation and performance tests, the gap kept stable. This may be due to the condition difference between the calculations and experiments.

In conclusion, it was believed that 2D model was considered as the good solution for OHP simulation. In order to fix the error of the simulation results, a fitting formula to consider the design parameters of OHP need to create for predicting the thermal performance of OHPs.
5.3 Correlation prediction of OHPs

For reducing the error of the simulation results, it needed a fitting formula to fix the gap between the simulation and the performance test. Considering the past prediction method mentioned by Khandekar (Khandekar et al., 2003), Katpradit (Katpradit et al., 2005), Charoensawan (Charoensawan et al., 2007), Arslan and Ozdemir (Arslan and Ozdemir, 2008), Sakulchangsatjatai (Sakulchangsatjatai et al., 2004), the dominating dimensionless parameters, including \( D/L \), \( Ja \), \( Bo \) and \( 1+(\rho_l/\rho_v)^{0.25} \), and some operating parameters including \( \Delta T \), \( Q \) were used to fix a correlation for predicting the heat transport capability of OHPs.

\[ \frac{D}{L} \] is the ratio of the inner diameter to that of the heat transfer length of the tube and it represents the geometry of the OHPs. The Jakob number \( (Ja=\frac{C_p AT}{h_{fg}}) \) is the ratio of sensible heat to that of the latent heat of the working fluid. The bond number \( (Bo=\frac{D_0}{L})(g(\rho_v-\rho_l))^{0.5} \) is the ratio of the buoyancy force to that of the surface tension force of the working fluid. The Wallis number \( (Wa=1+(\rho_l/\rho_v)^{0.25}) \) can be used to explain the flooding phenomenon that influences dry-out to occur at the evaporation section. \( \Delta T \) is the temperature difference between evaporation section and condensation section from the simulation results. \( Q \) is the power input.

According to the dimensionless method, the 2D simulation prediction of thermal resistance in vertical bottom heating mode was:

\[
R_r = 0.02669 \times \Delta T^{1.28803} \times Q^{1.25} \times [D/L]^{1.2577} \times [C_p AT/h_v]^{0.50135} \times [D_0 g(\rho_v-\rho_l)/g]^{0.50135}
\]

\[
\times [1+(\rho_l/\rho_v)^{0.25}]^{1.02677}
\]

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2D correlation prediction

performance test

\[ R_r = 0.02669 \times \Delta T^{1.28803} \times Q^{1.25} \times [D/L]^{1.2577} \times [C_p AT/h_v]^{0.50135} \times [D_0 g(\rho_v-\rho_l)/g]^{0.50135} \]

\[ \times [1+(\rho_l/\rho_v)^{0.25}]^{1.02677} \]


![Fig. 10](image_url) Comparison of measurement and prediction

As can be seen in Fig.10, R-square of 2D simulation prediction was 0.98175, which represents high reliability for the prediction fitting formula. The correlation prediction agrees with the experimental results fairly well.

(2) In order to reduce the error of the simulation results, the dimensionless method was used to create a fitting formula to fix the gap between the simulation and the performance test. The simulation correlation could predict the heat transport capability of OHPs successfully.

The 2D simulation prediction of thermal resistance in vertical bottom heating mode was:

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R_r = 0.02669 \times \Delta T^{1.28803} \times Q^{1.25} \times [D/L]^{1.2577} \times [C_p AT/h_v]^{0.50135} \times [D_0 g(\rho_v-\rho_l)/g]^{0.50135} \]

\[ \times [1+(\rho_l/\rho_v)^{0.25}]^{1.02677} \]

ACKNOWLEDGEMENTS

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NOMENCLATURE

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<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>Bo</td>
<td>Bond number ((=D_0g(\rho_v-\rho_l)/\sigma)^{0.5})</td>
</tr>
<tr>
<td>Cp</td>
<td>Constant specific heat ((\text{J/kg-K}))</td>
</tr>
<tr>
<td>D</td>
<td>Inner diameter ((\text{mm}))</td>
</tr>
<tr>
<td>D_L</td>
<td>Outer diameter ((\text{mm}))</td>
</tr>
<tr>
<td>g</td>
<td>Gravitational acceleration ((\text{m/s}^2))</td>
</tr>
<tr>
<td>h_v</td>
<td>Latent heat of vaporization ((\text{J/kg}))</td>
</tr>
<tr>
<td>T</td>
<td>Temperature difference between outlet and inlet ((=T_{17'}-T_{17}))</td>
</tr>
<tr>
<td>Ja</td>
<td>Jakob Number ((=C_p AT/h_v))</td>
</tr>
<tr>
<td>L</td>
<td>Heat transfer length ((\text{mm}))</td>
</tr>
<tr>
<td>L_e</td>
<td>Length of evaporation section ((\text{mm}))</td>
</tr>
<tr>
<td>L_c</td>
<td>Length of condensation section ((\text{mm}))</td>
</tr>
<tr>
<td>S</td>
<td>Heat transfer area ((\text{m}^2))</td>
</tr>
<tr>
<td>Wa</td>
<td>Wallis Number ((1+(\rho_l/\rho_v)^{0.25}))</td>
</tr>
<tr>
<td>Q</td>
<td>Power input ((\text{W}))</td>
</tr>
<tr>
<td>R</td>
<td>Thermal resistance of OHP ((\Omega/\text{W}))</td>
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Greek Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>( \rho )</td>
<td>Density ((\text{kg/m}^3))</td>
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<tr>
<td>( \sigma )</td>
<td>Surface tension ((\text{N/m}))</td>
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Subscripts

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<thead>
<tr>
<th>Symbol</th>
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<tbody>
<tr>
<td>c</td>
<td>Condensation section</td>
</tr>
<tr>
<td>e</td>
<td>Evaporation section</td>
</tr>
<tr>
<td>l</td>
<td>Liquid</td>
</tr>
<tr>
<td>v</td>
<td>Vapor</td>
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